#### Amendments to the Claims:

This listing of claims will replace all prior versions and listings of claims in the application.

#### **Listing of Claims:**

### 19. (New) A computer implemented process comprising:

obtaining a set of one or more private values  $Q_1, Q_2, ..., Q_m$  and respective public values  $G_1, G_2, ..., G_m$ , each pair of values  $(Q_i, G_i)$  verifying either the equation  $G_i \cdot Q_i^{\ \nu} \equiv 1 \, \text{mod} \, n$  or the equation  $G_i \equiv Q_i^{\ \nu} \, \text{mod} \, n$ , wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by  $p_1, ..., p_f$ , at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein  $\nu$  is a public exponent such that  $\nu = 2^k$ , and wherein k is a security parameter having an integer value greater than 1, and wherein each public value  $G_i$  (for i=1,...,m) is such that  $G_i \equiv g_i^{\ 2} \, \text{mod} \, n$ , wherein  $g_i$  (for i=1,...,m) is a base number having an integer value greater than 1 and smaller than each of the prime factors  $p_1,...,p_f$ , and  $g_i$  is a non-quadratic residue of the body of integers modulo n; and using at least the private values  $Q_1, Q_2, ..., Q_m$  in an authentication or in a signature method.

20. (New) The computer implemented process according to claim 19, further comprising:

receiving a commitment R from a demonstrator, the commitment R having a value computed such that:  $R = r^{\nu} \mod n$ , wherein r is an integer randomly chosen by the demonstrator;

choosing m challenges  $d_1, d_2, ..., d_m$  randomly;

sending the challenges  $d_1, d_2, ..., d_m$  to the demonstrator;

receiving a response D from the demonstrator, the response D having a value computed such that:  $D = r \times Q_1^{d_1} \times Q_2^{d_2} \times ... \times Q_m^{d_m} \mod n$ ; and

determining that the demonstrator is authentic if the response D has a value such that:  $D^{\nu} \times G_1^{\varepsilon_i d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n \text{ is equal to the commitment } R \text{, wherein, for } i=1,...,m,$   $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$ 

## 21. (New) The computer implemented process according to claim 19, further comprising:

receiving a commitment R from a demonstrator, the commitment R having a value computed using the Chinese remainder method from a series of commitment components  $R_j$ , the commitment components  $R_j$  having a value such that:  $R_j = r_j^{\nu} \mod p_j$  for j = 1,...,f, wherein  $r_1,...,r_f$  is a series of integers randomly chosen by the demonstrator;

choosing m challenges  $d_1, d_2, ..., d_m$  randomly;

sending the challenges  $d_1, d_2, ..., d_m$  to the demonstrator;

receiving a response D from the demonstrator, the response D being computed from a series of response components  $D_j$  using the Chinese remainder method, the response components  $D_j$  having a value such that:  $D_j = r_j \times Q_{1,j}^{-d_1} \times Q_{2,j}^{-d_2} \times ... \times Q_{m,j}^{-d_m} \mod p_j$  for j = 1,...,f, wherein  $Q_{i,j} = Q_i \mod p_j$  for i = 1,...,m and j = 1,...,f; and

determining that the demonstrator is authentic if the response D has a value such that:  $D^{\nu} \times G_1^{\varepsilon_i d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n \text{ is equal to the commitment } R \text{, wherein, for } i=1,...,m,$   $\varepsilon_i = +1 \text{ in the case } G_i \times Q_i^{\nu} = 1 \mod n \text{ and } \varepsilon_i = -1 \text{ in the case } G_i = Q_i^{\nu} \mod n.$ 

# 22. (New) The computer implemented process according to claim 19, further comprising:

receiving a token T from a demonstrator, the token T having a value such that T = h(M, R), wherein h is a hash function, M is a message received from the demonstrator, and R is a commitment having a value computed such that:  $R = r^{\nu} \mod n$ , wherein r is an integer randomly chosen by the demonstrator;

choosing m challenges  $d_1, d_2, ..., d_m$  randomly; sending the challenges  $d_1, d_2, ..., d_m$  to the demonstrator; receiving a response D from the demonstrator, the response D having a value such that:  $D = r \times Q_1^{d_1} \times Q_2^{d_2} \times ... \times Q_m^{d_m} \mod n$ ; and

determining that the message M is authentic if the response D has a value such that:  $h(M, D^{\nu} \times G_1^{\varepsilon_1 d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n)$  is equal to the token T, wherein, for i = 1,...,m,  $\varepsilon_i = +1$  in the case  $G_i \times Q_i^{\nu} = 1 \mod n$  and  $\varepsilon_i = -1$  in the case  $G_i = Q_i^{\nu} \mod n$ .

### 23. (New) The computer implemented process according to claim 19, further comprising:

receiving a token T from a demonstrator, the token T having a value such that T = h(M, R), wherein h is a hash function, M is a message received from the demonstrator, and R is a commitment having a value computed out of commitment components  $R_j$  by using the Chinese remainder method, the commitment components  $R_j$  having a value such that:  $R_j = r_j^{\ \nu} \mod p_j$  for j = 1,...,f, wherein  $r_1,...,r_f$  is a series of integers randomly chosen by the demonstrator;

choosing m challenges  $d_1, d_2, ..., d_m$  randomly;

sending the challenges  $d_1, d_2, ..., d_m$  to the demonstrator;

receiving a response D from the demonstrator, the response D being computed from a series of response components  $D_j$  using the Chinese remainder method, the response components  $D_j$  having a value such that:  $D_j = r_j \times Q_{1,j}^{-d_1} \times Q_{2,j}^{-d_2} \times ... \times Q_{m,j}^{-d_m} \mod p_j$  for j = 1,...,f, wherein  $Q_{i,j} = Q_i \mod p_j$  for i = 1,...,m and j = 1,...,f; and

determining that the message M is authentic if the response D has a value such that:  $h\left(M,D^{\nu}\times G_{1}^{\varepsilon_{i}d_{1}}\times G_{2}^{\varepsilon_{2}d_{2}}\times...\times G_{m}^{\varepsilon_{m}d_{m}} \mod n\right) \text{ is equal to the token } T \text{ , wherein, for } i=1,...,m \text{ , }$   $\varepsilon_{i}=+1 \text{ in the case } G_{i}\times Q_{i}^{\nu}=1 \mod n \text{ and } \varepsilon_{i}=-1 \text{ in the case } G_{i}=Q_{i}^{\nu} \mod n \text{ .}$ 

24. (New) The process according to claim 20, wherein the challenges are such that  $0 \le d_i \le 2^k - 1$  for i = 1,...,m.

25. (New) A process according to claim 19 for allowing a signatory to sign a message M, the method further comprising:

choosing m integers  $r_i$  randomly, wherein i is an integer between 1 and m; computing commitments  $R_i$  having a value such that:  $R_i = r_i^{\nu} \mod n$  for i = 1,...,m; computing a token T having a value such that  $T = h(M, R_1, R_2,...,R_m)$ , wherein h is a hash function producing a binary train consisting of m bits;

identifying the bits  $d_1, d_2, ..., d_m$  of the token T; and computing responses  $D_i = r_i \times Q_i^{d_i} \mod n$  for i = 1, ..., m.

26. (New) The process of claim 25, further comprising: collecting the token T and the responses  $D_i$  for i = 1,...,m; and

determining that the message M is authentic if the response D has a value such that:  $h(M, D^{\nu} \times G_1^{\varepsilon_1 d_1} \times G_2^{\varepsilon_2 d_2} \times ... \times G_m^{\varepsilon_m d_m} \mod n)$  is equal to the token T, wherein, for i = 1, ..., m,  $\varepsilon_i = +1$  in the case  $G_i \times Q_i^{\nu} = 1 \mod n$  and  $\varepsilon_i = -1$  in the case  $G_i = Q_i^{\nu} \mod n$ .

- 27. (New) A system used in a cryptographic process using asymmetric keys, the system comprising:
  - a memory storing a set of instructions; and
- a processor coupled to the memory for executing the set of instructions stored in the memory, the instructions including:

obtaining a set of one or more private values  $Q_1, Q_2, ..., Q_m$  and respective public values  $G_1, G_2, ..., G_m$ , each pair of keys  $(Q_i, G_i)$  verifying either the equation  $G_i \cdot Q_i^{\ \nu} \equiv 1 \bmod n$  or the equation  $G_i \equiv Q_i^{\ \nu} \bmod n$ , wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by  $p_1, ..., p_f$ , at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein f is a public exponent such that f is a security parameter having an integer value greater than 1, and wherein each public value f (for f is an integer value greater than 1, and wherein each public value f is a security parameter

is such that  $G_i \equiv g_i^2 \mod n$ , wherein  $g_i$  (for i = 1,...,m) is a base number having an integer value greater than 1 and smaller than each of the prime factors  $p_1,...,p_f$ , and  $g_i$  is a non-quadratic residue of the body of integers modulo n; and

using at least the private values  $Q_1, Q_2, ..., Q_m$  in an authentication or in a signature method.

28. (New) A computer readable medium containing computer code programmed for execution on multiple threads, the computer code comprising:

obtaining a set of one or more private values  $Q_1, Q_2, ..., Q_m$  and respective public values  $G_1, G_2, ..., G_m$ , each pair of keys  $(Q_i, G_i)$  verifying either the equation  $G_i \cdot Q_i^{\ \nu} \equiv 1 \, \text{mod} \, n$  or the equation  $G_i \equiv Q_i^{\ \nu} \, \text{mod} \, n$ , wherein m is an integer greater than or equal to 1, i is an integer between 1 and m, and wherein n is a public integer equal to the product of f private prime factors designated by  $p_1, ..., p_f$ , at least two of these prime factors being different from each other, wherein f is an integer greater than 1, and wherein  $\nu$  is a public exponent such that  $\nu = 2^k$ , and wherein k is a security parameter having an integer value greater than 1, and wherein each public value  $G_i$  (for i = 1, ..., m) is such that  $G_i \equiv g_i^{\ 2} \, \text{mod} \, n$ , wherein  $g_i$  (for i = 1, ..., m) is a base number having an integer value greater than 1 and smaller than each of the prime factors  $p_1, ..., p_f$ , and  $g_i$  is a non-quadratic residue of the body of integers modulo n; and

using at least the private values  $Q_1, Q_2, ..., Q_m$  in an authentication or in a signature method.